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# Mathematics <br> Paper 1 (Non-Calculator) <br> <br> Model Answers 

 <br> <br> Model Answers}

Higher Tier
4BNQMF"TTFTTNFOU.BUFSJBMTo*TTVF
Time: 1 hour 30 minutes
Paper Reference
1MA1/1H

You must have: Ruler graduated in centimetres and millimetres, Total Marks protractor, pair of compasses, pen, HB pencil, eraser.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
-     - there may be more space than you need.

Calculators may not be used.


- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.


## Information

The total mark for this paper is 80

- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## Answer ALL questions.

Write your answers in the spaces provided.
You must write down all the stages in your working.
1 Work out $6.34 \times 5.2$

$$
\begin{gathered}
(6.34 \times 5)+(6.34 \times 0.2) \\
\downarrow \\
(31.7)+(1.268)=32.968
\end{gathered}
$$

6.340
5.200
0.008
0.060
1.200
0.200
1.500
30.000
32.298

2 Expand and simplify $(m+7)(m+3)$

$$
\begin{aligned}
& m^{2}+7 m+3 m+21 \\
& =m^{2}+10 m+21
\end{aligned}
$$

3

$A E, D B G$ and $C F$ are parallel.
$D A=D B=D C$.
Angle $E A B=$ angle $B C F=38^{\circ}$
Work out the size of the angle marked $x$.
You must show your working.
$\angle A B D=38^{\circ}$ which $=B A D$
so $\angle B D A=180-(38 \times 2)=104^{\circ}$
The two triangles are the same so $\angle A D B+\angle C D B=104 \times 2=208^{\circ}$
$x=\angle C D A=(360-208)=152^{\circ}$

4 Gary drove from London to Sheffield.
It took him 3 hours at an average speed of $80 \mathrm{~km} / \mathrm{h}$.
Len drove from London to Sheffield.
She took 5 hours.
Assuming that Len

drove along the same roads as Gary and did not take a break,
(a) work out Len's average speed from London to Sheffield.

First need Gary distance $\rightarrow$ speed $\times$ time $\rightarrow 80 \times 3=240 \mathrm{~km}$
Lan speed $\rightarrow \frac{\text { distance }}{\text { time }} \rightarrow \frac{240}{5}=48 \mathrm{~km} / \mathrm{h}$
(b) If Len did not drive along the same roads as Gary, explain how this could affect your answer to part (a).

She would then have driven a different distance to Gary
and so her average speed would be different

5 In a company, the ratio of the number of men to the number of women is $3: 2$
$40 \%$ of the men are under the age of 25
$10 \%$ of the women are under the age of 25
What percentage of all the people in the company are under the age of 25 ?
Tole ratio $=3+2=5$
40.1. of men $\rightarrow 0.4 \times 3=1.2$

10 1. of women $\rightarrow 0.1 \times 2=0.2$


28 \%

6 The plan, front elevation and side elevation of a solid prism are drawn on a centimetre grid.

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|  |  | front elevation |  |  |  | side elevation |  |  |  |  |  |  |

In the space below, draw a sketch of the solid prism.
Write the dimensions of the prism on your sketch.


7 There are 1200 students at a school.
Kate is helping to organise a party.
She is going to order pizza.
Kate takes a sample of 60 of the students at the school.
She asks each student to tell her one type of pizza they want.
The table shows information about her results.

| Pizza | Number of students |
| :---: | :---: |
| ham | 20 |
| salami | 15 |
| vegetarian | 8 |
| margarita | 17 |

Work out how much ham pizza Kate should order.
Write down any assumption you make and explain how this could affect your answer.

$$
\left(\frac{1200}{60}\right) \times 20 \mathrm{ham}=(20) \times 20=400 \mathrm{ham} \text { pizzas }
$$

I assumed the sample is representative of the population.

8 Here is a parallelogram.


Work out the value of $x$ and the value of $y$.
Opposite sides of parallelogram are equal so $\begin{aligned} 5 x-20 & =2 x+43 \\ 3 x & =63 \\ x & =21\end{aligned}$
Total angle value of parallelogram $=360^{\circ}$. So $360^{\circ}=(5 x-20)+(2 x+43)+2(4 y-5 x)$

$$
\begin{aligned}
& 360^{\circ}=(85)+(85)+85-10 x \\
& 360^{\circ}=170^{\circ}+8 y-210^{\circ} \\
& 360^{\circ}=85-40^{\circ} \\
& 400^{\circ}=85 \\
& 50^{\circ}=y
\end{aligned}
$$

$$
x=\quad 21^{\circ}
$$

9 Work out the value of $\left(9 \times 10^{-4}\right) \times(3 \times 10$
${ }^{7}$ ) Give your answer in standard form.

$$
(9 \times 3) \times\left(10^{-4} \times 10^{7}\right) \rightarrow\left(27 \times 10^{3}\right) \rightarrow\left(2.7 \times 10^{4}\right)
$$

10 (a) Write down the value of 64

$$
64^{1 / 2} \rightarrow \sqrt{64}=8
$$

(b) Find the value of $\frac{8}{125}^{-\frac{2}{3}}$ 125
$\left(\frac{8}{125}\right)^{-2 / 3} \rightarrow\left(\frac{8}{125}\right)^{3 / 2} \rightarrow\left(\sqrt[3]{\frac{8}{125}}\right)^{2} \rightarrow\left(\frac{2}{5}\right)^{2} \rightarrow \frac{4}{25}$

11 One uranium atom has a mass of $3.95 \times 10^{-22}$ grams.
(a) Work out an estimate for the number of uranium atoms in 1 kg of uranium.

Estimate so $4 \times 10^{-22}$.
$\begin{aligned} \frac{10009}{4 \times 10^{-22} 9} \rightarrow\left(1 \times 10^{3}\right) \div\left(4 \times 10^{-22}\right) & \rightarrow(1 \div 4) \times\left(10^{3} \div 10^{-22}\right) \\ & =(0.25) \times\left(10^{25}\right) \\ & =2.5 \times 10^{24}\end{aligned}$
(b) Is your answer to (a) an underestimate or an overestimate?

Give a reason for your answer.
Underestimate as I rounded op the number however it
was in the denominator. $\qquad$

12 Pressure = force/area
Find the pressure exerted by a force of 900 newtons on an area of $60 \mathrm{~cm}^{2}$.
Give your answer in newtons $/ \mathrm{m}^{2}$.

$$
\begin{aligned}
& 60 \mathrm{~cm} \xrightarrow{\div 100} 0.6 \mathrm{~m} \\
& 60 \mathrm{~cm}^{2} \xrightarrow{\div 10000} 0.006 \mathrm{~m}^{2}
\end{aligned}
$$

$$
\frac{900}{0.006}=
$$

0.006 soesinte 61000 times into $600 \quad 100000$ times into 900 150,000 times

newtons $/ \mathrm{m}^{2}$
(Total for Question 12 is 2 marks)

13 Rectangle $A B C D$ is mathematically similar to rectangle $D A E F$.

$A B=10 \mathrm{~cm}$.
$A D=4 \mathrm{~cm}$.
Work out the area of rectangle $D A E F$.
Scale factor $\rightarrow 4 / 10=0.4$
$4 \times 0.4=D F=1.6 \mathrm{~cm}$
$1.6 \times 4=6.4 \mathrm{~cm}^{2}$
6.4
$\mathrm{cm}^{2}$

14 Ben played 15 games of basketball.
Here are the points he scored in each game.

| 17 | 18 | 18 | 18 | 19 | 20 | 20 | 22 | 23 | 23 | 23 | 26 | 27 | 28 | 28 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(a) Draw a box plot for this information.


Sam plays in the same 15 games of basketball.
The median number of points Sam scored is 23
The interquartile range of these points is 12
The range of these points is 20
(b) Who is more consistent at scoring points, Sam or Ben?

You must give a reason for your answer.

Ben is more ronsistut as IQR is 8 which is less than Jams IQR of 12 - So Ben has a Small spread of data ad is more consistent. His range is also less (II) than $\operatorname{sam}(20)$.

15 In a shop, all normal prices are reduced by $20 \%$ to give the sale price.
The sale price of a TV set is then reduced by $30 \%$.
Mary says,
" $30+20=50$, so this means that the normal price of the TV set has been reduced by $50 \%$."

Is Mary right?
You must give a reason for your answer.

No, because the fetal reduction is $0.8 \times 0.7=0.44$. This means the fotal reduction is 44-1- and not 50.1.

16 Factorise fully $20 x^{2}-5$

$$
20 x^{2}-5 \rightarrow 5\left(4 x^{2}-1\right) \rightarrow 5(2 x-1)(2 x+1)
$$

## $5(2 x-1)(2 x+1)$

(Total for Question 16 is 2 marks)
17 Make $a$ the subject of $\quad a+3=\frac{2 a+7}{r}$

$$
\begin{aligned}
+3=\frac{2 a+7}{r} \rightarrow r(a+3)=2 a+7 \rightarrow & a r+3 r=2 a+7 \\
& \text { ar }-2 a=7-3 r \\
& a(r-2)=7-3 r \\
& a=\frac{7-3 r}{r-2}
\end{aligned}
$$

$$
a=\frac{7-3 r}{r-2}
$$

18 Solid A and solid B are mathematically similar.
The ratio of the surface area of solid $\mathbf{A}$ to the surface area of solid $\mathbf{B}$ is 4:9
The volume of solid $\mathbf{B}$ is $405 \mathrm{~cm}^{3}$.
Show that the volume of solid $\mathbf{A}$ is $120 \mathrm{~cm}^{3}$.


19 Solve $x^{2}>3 x+4$

$$
\begin{array}{r}
x^{2}>3 x+4 \rightarrow \quad x^{2}-3 x-4>0 \\
(x-4)(x+1)>0 \\
x>4 \quad x<-1
\end{array}
$$


(a) Enlarge shape $\mathbf{A}$ by scale factor -2 , centre $(0,0)$

Label your image $\mathbf{B}$.
(b) Describe fully the single transformation that will map shape $\mathbf{B}$ onto shape $\mathbf{A}$.

Enlargement by scale factor - 0.5 from centre $(0,0)$.

21 Here is a speed-time graph for a car journey.
The journey took 100 seconds.


The car travelled 1.75 km in the 100 seconds.
(a) Work out the value of $V$.

Area of graph is distance $=1750 \mathrm{~m}$
$1750=10 \mathrm{v}+40 \mathrm{v}+20 \mathrm{v}$
$1750=70 \mathrm{~V}$
$\frac{1750}{70}=v-25$
$v=25$
(3)
(b) Describe the acceleration of the car for each part of this journey.

First stage acceleration $\rightarrow \frac{25}{20}=1.25 \mathrm{~ms}^{-2}$

Second stage no accelvation (constant speed) $=0 \mathrm{~ms}^{-2}$

Final stage deceleration $\frac{25}{40}=-0.625 \mathrm{~ms}^{-2}$
(Total for Question 21 is 5 marks)

22 Bhavna recorded the lengths of time，in hours，that some adults watched TV last week．
The table shows information about her results．

| Length of time $(\boldsymbol{t}$ hours $)$ | Frequency |
| :---: | :---: |
| $0 《<t<10$ | 6 |
| $10 《<t<15$ | 8 |
| $15 《<t<20$ | 15 |
| $20 \ll t<40$ | 5 |

Bhavna made some mistakes when she drew a histogram for this information．


Write down two mistakes Bhavna made．
1 Areas are not equal to trequacies in fable

2 Final bar has wrong width of 50．Should be 40

23 Show that $\frac{1}{1}$ can be written as $2-\downarrow$

$$
1+\frac{1}{\sqrt{2}}
$$

$$
\left(1+\frac{1}{\sqrt{2}}\right) \rightarrow \frac{\sqrt{2}}{\sqrt{2}}+\frac{1}{\sqrt{2}} \rightarrow \frac{\sqrt{2}+1}{\sqrt{2}}
$$

$$
1 \div \frac{\sqrt{2}+1}{\sqrt{2}} \rightarrow 1 \times \frac{\sqrt{2}}{\sqrt{2}+1} \rightarrow \frac{\sqrt{2}}{\sqrt{2}+1}
$$

$$
\frac{\sqrt{2} \times(\sqrt{2}-1)}{(\sqrt{2}+1) \times(\sqrt{2}-1)} \rightarrow \frac{2-\sqrt{2}}{2-1} \rightarrow 2-\sqrt{2}
$$

24 John has an empty box.
He puts some red counters and some blue counters into the box.
The ratio of the number of red counters to the number of blue counters is $1: 4$
Linda takes at random 2 counters from the box. The
probability that she takes 2 red counters is $6 / 155$
How many red counters did John put into the box?
$\frac{x}{5 x}$ red $\frac{4 x}{5 x}$ slue
$\frac{x}{5 x} \times \frac{x-1}{5 x-1}=\frac{6}{155}$
$\begin{aligned} & \frac{x^{2}-x}{25 x^{2}-5 x}=\frac{6}{155} \rightarrow \begin{array}{l}155 x^{2}-155 x \\ 155 x-155\end{array}=150 x^{2}-30 x \\ &=150 x-30\end{aligned}$
$5 x=125$
$x=25$

## 25

$25 A(-2,1), B(6,5)$ and $C(4, k)$ are the vertices of a right-angled triangle $A B C$.
Angle $A B C$ is the right angle.
Find an equation of the line that passes through $A$ and $C$.
Give your answer in the form $a y+b x=c$ where $a, b$ and $c$ are integers.


Gradient of $A B \rightarrow \frac{S-1}{6--2}=\frac{4}{8}=1 / 2$
So gradient of perpendicular $B C$ is $-2 \rightarrow y=-2 x+c$
$B C$ goes though point $B$ so $\rightarrow(5)=-2(6)+C \rightarrow S=-12+C \rightarrow \leq=17$
BC $\rightarrow y=-2 x+17$
we know point $C$ 's $x$ is 4 so substitute in $B C \rightarrow y=-2(4)+17 \rightarrow y=9$
Point $C$ is $(4,9)$

Line ENough A $(-2,1)$ and $<(4,9)$
Gradient $\frac{9-1}{4--2}=\frac{8}{6}=4 / 3 \rightarrow b=4 / 3 x+c$
Goes though $C$ so sub in $\rightarrow 9=4 / 3(4)+C \rightarrow C=9-\frac{16}{3}=11 / 3$ $y=413 x+11 / 3$ is line $A C$
$\rightarrow 3 y-4 x=11$

